## Chomp



Julia Robinson Mathematics Festival

## Chomp

## Objective:

The winner is the player who doesn't eat the yucky square.

## Rules:

- Players take turns eating chocolate squares.
- When a square is eaten, all squares above and to the right of that square are also eaten.
- The player who is forced to eat the yucky square loses.


Blue must eat the yucky square, so yellow wins!
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## Square Bars

1. Start with a $3 \times 3$ chocolate bar and play a few games. Does Player 1 or Player 2 usually win?
2. When it's your turn, are there any shapes that you have a winning strategy for? What about shapes that you're pretty sure mean you will lose?
3. Can you find a strategy that helps Player 1 or Player 2 win every time?
4. Does this same strategy work for $4 \times 4$ bars? $5 \times 5$ bars? Any $n \times n$ bar?


## Narrow Bars

1. Now start with a $2 \times 4$ chocolate bar and play a few games. Does Player 1 or Player 2 usually win?
2. When it's your turn, are there any shapes that you have a winning strategy for? What about shapes that you're pretty sure mean you will lose?
3. Can you find a strategy that helps Player 1 or Player 2 win every time?
4. Does this same strategy work for $2 \times 5$ bars? $2 \times 6$ bars? Any $2 \times n$ bar?


## $3 \times 4$ Bars

1. Now start with a $3 \times 4$ chocolate bar and play a few games. Does Player 1 or Player 2 usually win?
2. When it's your turn, are there any shapes that you have a winning strategy for? What about shapes that you're pretty sure mean you will lose? (You might recognize some from before!)
3. Can you find a strategy that helps Player 1 or Player 2 win every time? (This is a good deal more complicated than the other bars we've looked at and will likely require careful note-taking!)


## Bigger Bars

What can you say about bigger bars? $3 \times n$ ? $4 \times 5$ ? $m \times n$ ?
While you probably found nice strategies for square bars or $2 x n$ bars that weren't too hard to explain to a friend, you might have a little more trouble telling a friend how to win on a $3 \times 4$ bar without telling them exactly what to do in a bunch of different cases. Mathematicians still haven't found a nice way to describe winning strategies for the $3 x n$ family of bars, if such "nice" strategies even exist! Are there any other families of chocolate bars you can find nice, somewhat easy-to-explain strategies for?


